Assignment #4

Math 180

Name:

1. Using Product Rule of derivative to prove that

$$\frac{d}{dx}(f(x)g(x)h(x)) = \frac{df}{dx}g(x)h(x) + f(x)\frac{dg}{dx}h(x) + f(x)g(x)\frac{dh}{dx}$$

2. Differentiate the following functions. (No need to simplify) a) $f(x) = (3x^2 - 5x + 4)(2x^3 + x^2 - 2)$

b)
$$f(x) = \frac{7x^3 - 5x + 2}{4x^3 - 2x + 7}$$

3. Find the equation of the tangent line to the given curve at the specific point.

a)
$$f(x) = \frac{7x^2 - 2x + 4}{3x^3 - 2x + 2}; at x = 1$$

b)
$$f(x) = e^{x} (7x^{3} - 5x^{2} + 2); at x = 0$$

- 4. A particle moves according to the law of motion $s = f(t) = t^3 8t^2 + 5t + 2$
 - a) Find the velocity and acceleration of the particle at time t.
 - b) What is the velocity at t = 3, 7.
 - c) When is the particle at rest?
 - d) When is the particle moving in the positive / negative direction?
 - e) Find the total distance traveled during the first 8 seconds.
 - f) Draw a diagram to illustrate the motion of the particle.

- 5. If a ball is thrown vertically upward with a velocity of 80 ft/s, then its height after t seconds is $s = 80t 16t^2$.
 - a) What is the maximum height reached by the ball?
 - b) What is the velocity of the ball when it is 96 ft above the ground on its way up and on its way down?
 - c) Find the impact speed of the ball when it hits the ground.