

Assignment #4**Math 260****Name:**

1. Prove / disprove if the following set is a vector space. Provide counter example for not a vector space.

a) $S = \left\{ \begin{bmatrix} a & c \\ b & d \end{bmatrix} \mid a+2b=c-3d \right\}$

b) $S = \left\{ \begin{bmatrix} x \\ y \end{bmatrix} \in R^2 \mid xy \geq 0 \right\}$

c) $S = \left\{ A \in M_2(R) \mid \det(A) = 0 \right\}$

$$\text{d)} \quad S = \left\{ f(x) = ax^2 + bx + c \in P_2 \mid f(0) + 2f'(0) = 0 \right\}$$

$$\text{e)} \quad S = \left\{ A \in M_2(R) \mid A = A^T \right\}$$

2. Determine if S is a subspace of a vector space V.

a) $S = \left\{ \begin{bmatrix} a \\ b \\ c \end{bmatrix} \in V = R^3 \mid \int_0^1 (ax^2 + bx + c) dx = 0 \right\}$

b) $S = \left\{ A \in M_2(R) \mid A^2 + A = I_2 \right\}$

c) $S = \left\{ \begin{bmatrix} a \\ b \\ c \end{bmatrix} \in R^3 \mid a + 2b + 3c = 1 \right\}$

d) All points on the unit circle: $S = \{(x, y) \in R^2 \mid x^2 + y^2 = 1\}$

e) $S = \{A \in M_3(R) \mid \text{tr}(A) = 0\}$

f) Set of all non-singular matrices: $S = \{A \in V = M_n(R) \mid \det(A) \neq 0\}$