

1. Integrate the following:

a) $\int (3x^3 - 2x + 7)e^{2-3x} dx$

b) $\int (7x^3 - 5x^2 - 4)\sin(3x) dx$

c) $\int (\sqrt[3]{x^2} - 3\sqrt{x} - 2)\ln(4x) dx$

d) $\int \sin^{-1}(4x) dx$

e) $\int e^{3x+2} \cos(5x) dx$

f) $\int \ln(4x-3) dx$

g) $\int x \tan^{-1}(3x) dx$

h) $\int e^{\sqrt{x}} dx$

i) $\int \sin(\ln x) dx$

2. Prove the following reduction formulas:

a)
$$\int \cos^n x dx = \frac{1}{n} \cos^{n-1} x \sin x + \frac{n-1}{n} \int \cos^{n-2} x dx$$

b)
$$\int (\ln x)^n dx = x(\ln x)^n - n \int (\ln x)^{n-1} dx$$

c)
$$\int \sec^n(x) dx = \frac{\sec^{n-2} x \tan x}{n-1} + \frac{n-2}{n-1} \int \sec^{n-2} x dx$$

3. Use problem (2) to evaluate the following:

a) $\int \cos^5(5x) dx$

c) $\int [\ln(5x)]^3 dx$

d) $\int \sec^5(4x) dx$