

1. Solve the following differential equations:

a)
$$\frac{dy}{dx} = \frac{e^{2-x-3y}}{e^{3x+y+1}}$$

b)
$$\frac{dy}{dx} = x^2 y^2 - 5xy^2 + y^2$$

c) $\frac{dy}{dx} = \frac{x^2 y - 32}{16 - x^2} + 2$

d) $\frac{dy}{dx} = y^3 \sin x; y(0) = 1$

e) $\frac{dy}{dx} = \frac{2}{3}(y-1)^{1/2}; y(1) = 1$

f) $\frac{dy}{dx} = y^2 - 3y - 10$

2. A tank contains 500 gallons of brine with 4 lbs of dissolved salt. Brine that contains 0.2 lbs of salt per gallon enters the tank at a rate of 4 gal/min. The solution is kept thoroughly mixed and drains from the tank at the same rate of 4 gal/min.
- a) Set up an IVP for the amount of salt $A(t)$ as a function of time t (in minutes)
 - b) Determine the concentration of the salt in the tank after one hour.

3. Set up an IVP for a mortgage loan of \$650,000 at interest rate of 4.5% per year for 30 years. Then determine the monthly payment of the loan and the total interest amount after 30 years.