

1. Solve the following DE:

a) $(2y^2e^{2x} + 3x^2)dx + 2ye^{2x}dy = 0$

b) $\left(\frac{1}{x} - \frac{y}{x^2 + y^2}\right)dx + \frac{x}{x^2 + y^2}dy = 0$

c) $\left[1 + \ln(xy)\right]dx + xy^{-1}dy = 0$

d) $(2xy + \cos y)dx + (x^2 - x \sin y - 2y)dy = 0$

e) $(3x^2 \ln x + x^2 - y)dx - xdy = 0; y(1) = 5$

f) $(ye^{xy} + \cos x)dx + xe^{xy}dy = 0; y\left(\frac{\pi}{2}\right) = 0$

2. Determine an integrating factor for the given differential equation, and hence find the general solution

a) $(3xy - 2y^{-1})dx + x(x + y^{-2})dy = 0$

b) $x^2ydx + y(x^3 + e^{-3y} \sin y)dy = 0$